Maths Assignment

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B.E. MECHANICAL

1. The maximum weight that an elevator in an apartment complex can accommodate is 800kg. The average adult weight be about 70 kgs with a variance of 200. What is the probability that the in safely reaches the ground when there are 10 adults in the lift?

Solution:

Given :

- The maximum weight that an elevator can accommodate is 800kg. The average adult weight be about 70 kgs with a variance of 200.

- It is given that there are 10 adults in the elevator whose each adult's average weight is 70kgs.

- So, 10\*70=700

And the maximum weight an elevator can accommodate is 800kg.

- Still 100 kgs of weight is left.

So yes, the elevator can reach the ground safely.

Given mean= 70

variance = 200

hence mean for 10 adults = 10\*70= 700

variance for 10 adults = 10\*200= 2000

therefore standard deviation SD = sqrt(2000)​ = 44.72

If the weight > 800 kg causes the elevator to "unsafely" reach the ground, then we can find the upper tail of our normal distribution:

P(Weight of 10 adults > 800 kg).

Z-score =(X-mu)/SD =(800-700)/44.72 = 2.24

Hence P (Z <2.24), using z table we get 0.9875 or 98.75%

Hence it is safe to reach the ground when there are 10 adults in the lift.

1. The life of a 60-watt light bulb in hours is known to be norm distributed with σ =25 hours. Create 5 different random samples of 100 bulbs each which has a mean life of x\_bar˜1000 hours and perform one-way ANOVA with state it.

Solution:

The total sample size is N=5\*100=500

Therefore, the total degrees of freedom are

dftotal​=500−1=499

The between groups degrees of freedom are

dfbetween​=5−1=4

And the within-groups degrees of freedom are

dfwithin​=dftotal​−dfbetween​=499−4=495

∑​Xij​=499712

(∑​Xij​)2=499691630

SStotal​=(∑​Xij​)2​−1/N(∑​Xij​)2=267464.112

SSwithin​=266084.42

​SSbetween​=1379.692​

MSbetween​= ​SSbetween/dfbetween ​​=1379.692/4​=344.923

MSwithin​= ​SSwithin/dfwithin ​​=266084.42/495​=537.544

F= ​MSbetween/MSwithin ​​=344.923/537.544​/=0.642

The following null and alternative hypotheses need to be tested:

H0​:μ1​=μ2​=μ3​=μ4​=μ5​

H1​: Not all means are equal.

The above hypotheses will be tested using an F-ratio for a One-Way ANOVA.

Based on the information provided, the significance level is α=0.05, and the degrees of freedom are df1​=4 and df2​=4, therefore, the rejection region for this F-test is R={F:F>Fc​=2.39}.

Test Statistics

F= ​MSbetween/MSwithin ​​=344.923/537.544​=0.642

Since it is observed that F=0.642<2.39=Fc​, it is then concluded that the null hypothesis is not rejected. Therefore, there is not enough evidence to claim that not all 5 population means are equal, at the α=0.05 significance level.

Using the P-value approach: The p-value is p=0.633 and since p=0.633≥0.05, it is concluded that the null hypothesis is not rejected. Therefore, there is not enough evidence to claim that not all 5 population means are equal, at the α=0.05 significance level.

1. Fifteen trainees in a technical program are randomly assigned to three different types of instructional approaches, all of which are concerned with developing specified level of skill in computer-assisted design. The achievement test scores at the conclusion of the instructional unit are reported in Table along with the mean Performance score associated with each instructional approach. Use the analysis of variance procedure to test the null hypothesis that the three-sample means were obtained from the same population, using the 5 percent level of significance for the test.

|  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- |
| Instrumental method | Test scores | | | | | Total scores | Mean test scores |
| A1 | 86 | 79 | 81 | 70 | 84 | 400 | 80 |
| A2 | 90 | 76 | 88 | 82 | 89 | 425 | 85 |
| A3 | 82 | 68 | 73 | 71 | 81 | 375 | 75 |

Solution:

We have 15 students A1, A2, A3

α=0.05

H0​: μ1​=μ2​=μ3​

H1​: at least one of the means is different.

From excel ANOVA calculations

|  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- |
| Anova: Single Factor |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| SUMMARY |  |  |  |  |  |  |
| *Groups* | *Count* | *Sum* | *Average* | *Variance* |  |  |
| Row 1 | 5 | 400 | 80 | 38.5 |  |  |
| Row 2 | 5 | 425 | 85 | 35 |  |  |
| Row 3 | 5 | 375 | 75 | 38.5 |  |  |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |
| ANOVA |  |  |  |  |  |  |
| *Source of Variation* | *SS* | *df* | *MS* | *F* | *P-value* | *F crit* |
| Between Groups | 250 | 2 | 125 | 3.348214 | 0.069909 | 3.885294 |
| Within Groups | 448 | 12 | 37.33333 |  |  |  |
|  |  |  |  |  |  |  |
| Total | 698 | 14 |  |  |  |  |

The F value calculated was 3.34. This is less than the stated critical value (Fcrit) of 3.88, and the probability of obtaining this result by chance (P-value) was calculated as 0.0699 (6.99% to three significant figures). We conclude that there was not a significant difference in means and the three-sample means were obtained from the same population, since P >0.05.

Alternative method by manual calculations:

n = 5 replications

a = 3 treatment

alpha, a = 0.05

overall mean 80μ=380+85+75​=80

SS treatment = 5×[(80−80)2+(85−80)2+(75−80)2]

SS treatment = 250

SS total = [(86−80)2+(79−80)2+(81−80)2+(70−80)2+(84−80)2+(90−80)2+(76−80)2+(88−80)2+(82−80)2+(89−80)2+(82−80)2+(68−80)2+(73−80)2+(71−80)2+(81−80)2]

SS total = 698

SSE = SS total - SS treatment

SSE = 448

MS treatment =SStreatment/(a−1)=125

MSE = SSE/ a(n−1)​=37.333

F0​=MStreatment/MSE

​F0​=3.348

critical value = F(a,a-1,a(n-1)) = F(0.05,2,12) = 3.89

since F0<3.89 hence null hypothesis can not be rejected

Hence we conclude that the three sample means were obtained from the same population.